

10.1 For $s < t < u$ we have

$$\begin{aligned}
 \mathbf{E}_s [\varepsilon_t] &= \mathbf{E}_s [\mathbf{E}_{t-1} [\varepsilon_t]] = \mathbf{E}_s [0] = 0 & (1) \\
 \text{Var}_s (\varepsilon_t) &= \mathbf{E}_s [\varepsilon_t^2] - (\mathbf{E}_s [\varepsilon_t])^2 \stackrel{(1)}{=} \mathbf{E}_s [\varepsilon_t^2] \\
 &\stackrel{\text{LawIE}}{=} \mathbf{E}_s [\mathbf{E}_{t-1} [\varepsilon_t^2]] \stackrel{(1)}{=} \mathbf{E}_s [\mathbf{E}_{t-1} [\varepsilon_t^2] - (\mathbf{E}_{t-1} [\varepsilon_t])^2] \\
 &= \mathbf{E}_s [\text{Var}_{t-1} (\varepsilon_t)] = \mathbf{E}_s [1] = 1 \\
 \text{Var}_s (\varepsilon_t, \varepsilon_u) &= \mathbf{E}_s [(\varepsilon_t - \mathbf{E}_s [\varepsilon_t]) (\varepsilon_u - \mathbf{E}_s [\varepsilon_u])] \\
 &\stackrel{(1)}{=} \mathbf{E}_s [\varepsilon_t \varepsilon_u] \stackrel{\text{LawIE}}{=} \mathbf{E}_s [\mathbf{E}_t [\varepsilon_t \varepsilon_u]] \stackrel{\text{LawCC}}{=} \mathbf{E}_s [\varepsilon_t \mathbf{E}_t [\varepsilon_u]] \\
 &= \mathbf{E}_s [\varepsilon_t \times 0] = 0
 \end{aligned}$$