

10.5 (a)

$$\begin{aligned} d(B_t^2 - t) &= 2B_t dB_t + \frac{1}{2} 2\text{Var}_t(dB_t) - dt \\ &= 2B_t dB_t \end{aligned}$$

(b)

$$\begin{aligned} d(B_t^3 - t B_t) &= 3B_t^2 dB_t + \frac{1}{2} 6B_t \text{Var}_t(dB_t) - B_t dt - t dB_t \\ &= 2B_t dt + (3B_t^2 - t) dB_t \end{aligned}$$

(c)

$$\begin{aligned} de^{B_t} &= e^{B_t} dB_t + \frac{1}{2} e^{B_t} \text{Var}_t(dB_t) \\ &= e^{B_t} dB_t + \frac{1}{2} e^{B_t} dt. \end{aligned}$$