

**B.24** We would like to find a linear transform of the vector  $\varepsilon = [\varepsilon_1 \ \varepsilon_2 \ \varepsilon_3]$  such that  $A\varepsilon$  has variance-covariance matrix  $\Sigma$ . By construction the variance-covariance matrix of  $\varepsilon$  is an identity matrix. By the portfolio theorem for covariances

$$\Sigma_{A\varepsilon} = A\Sigma_{\varepsilon}A^* = AA^*.$$

Hence we need to find  $A$  such that  $AA^* = \Sigma$ . But we already have such a matrix in the form of the lower triangular matrix of the Cholesky decomposition, because  $\sigma\sigma^* = \Sigma$ ! So it is enough to take the matrix of the generated values  $\varepsilon_{\text{data}}$  and multiply it from the right by  $\sigma^*$ . The resulting series will have population variance-covariance matrix equal to  $\Sigma$ . Finally we add the mean to obtain the return series  $IF$  (this works because adding a constant does not change the variances or covariances). Try this, starting with EXCEL spreadsheet *ExeB\_24.xls*. For a solution see the EXCEL spreadsheet *ExeB\_24Sol.xls*.